Progression Document for Maths - Brabin's Endowed Primary School

Purpose of study

Mathematics is a creative and highly inter-connected discipline that has been developed over centuries, providing the solution to some of history's most intriguing problems. It is essential to everyday life, critical to science, technology and engineering, and necessary for financial literacy and most forms of employment. A high-quality mathematics education therefore provides a foundation for understanding the world, the ability to reason mathematically, an appreciation of the beauty and power of mathematics, and a sense of enjoyment and curiosity about the subject.

Aims

The national curriculum for mathematics aims to ensure that all pupils:

- become fluent in the fundamentals of mathematics, including through varied and frequent practice with increasingly complex problems over time, so that pupils develop conceptual understanding and the ability to recall and apply knowledge rapidly and accurately.
- reason mathematically by following a line of enquiry, conjecturing relationships and generalisations, and developing an argument, justification or proof using mathematical language
- can solve problems by applying their mathematics to a variety of routine and non-routine problems with increasing sophistication, including breaking down problems into a series of simpler steps and persevering in seeking solutions.

EYFS

Mathematics is a specific area of learning and development in the EYFS which has two aspects: Number and Numerical Patterns.

"Developing a strong grounding in number is essential so that all children develop the necessary building blocks to excel mathematically. Children should be able to count confidently, develop a deep understanding of the numbers to 10, the relationships between them and the patterns within those numbers. By providing frequent and varied opportunities to build and apply this understanding - such as using manipulatives, including small pebbles and tens frames for organising counting - children will develop a secure base of knowledge and vocabulary from which mastery of mathematics is built. In addition, it is important that the curriculum includes rich opportunities for children to develop their spatial reasoning skills across all areas of mathematics including shape, space and measures. It is important that children develop positive attitudes and interests in mathematics, look for patterns and relationships, spot connections, 'have a go', talk to adults and peers about what they notice and not be afraid to make mistakes." DfE Statutory framework for the early years foundation stage

By the end of the Reception year, children at the expected level of development will: ELG: Number

- Have a deep understanding of number to 10, including the composition of each number; 14

- Subitise (recognise quantities without counting) up to 5;

- Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 (including subtraction facts) and some number bonds to 10, including double facts. ELG: Numerical Patterns

- Verbally count beyond 20, recognising the pattern of the counting system;
- Compare quantities up to 10 in different contexts, recognising when one
- augntity is areater than, less than or the same as the other augntity;
- Explore and represent patterns within numbers up to 10, including evens and

odds, double facts and how quantities can be distributed equally.

KS1

The principal focus of mathematics teaching in key stage 1 is to ensure that pupils develop confidence and mental fluency with whole numbers, counting and place value. This should involve working with numerals, words and the four operations, including with practical resources [for example, concrete objects and measuring tools].

At this stage, pupils should develop their ability to recognise, describe, draw, compare and sort different shapes and use the related vocabulary. Teaching should also involve using a range of measures to describe and compare different quantities such as length, mass, capacity/volume, time and money.

By the end of year 2, pupils should know the number bonds to 20 and be precise in using and understanding place value. An emphasis on practice at this early stage will aid fluency. Pupils should read and spell mathematical vocabulary, at a level consistent with their increasing word reading and spelling knowledge at key stage 1.

LKS2

The principal focus of mathematics teaching in lower key stage 2 is to ensure that pupils become increasingly fluent with whole numbers and the four operations, including number facts and the concept of place value. This should ensure that pupils develop efficient written and mental methods and perform calculations accurately with increasingly large whole numbers. At this stage, pupils should develop their ability to solve a range of problems, including with simple fractions and decimal place value. Teaching should also ensure that pupils draw with increasing accuracy and develop mathematical reasoning so they can analyse shapes and their properties, and confidently describe the relationships between them. It should ensure that they can use measuring instruments with accuracy and make connections between measure and number.

By the end of year 4, pupils should have memorised their multiplication tables up to and including the 12 multiplication table and show precision and fluency in their work. Pupils should read and spell mathematical vocabulary correctly and confidently, using their growing word reading knowledge and their knowledge of spelling.

<u>UKS2</u>

The principal focus of mathematics teaching in upper key stage 2 is to ensure that pupils extend their understanding of the number system and place value to include larger integers. This should develop the connections that pupils make between multiplication and division with fractions, decimals, percentages and ratio.

At this stage, pupils should develop their ability to solve a wider range of problems, including increasingly complex properties of numbers and arithmetic, and problems demanding efficient written and mental methods of calculation. With this foundation in arithmetic, pupils are introduced to the language of algebra as a means for solving a variety of problems. Teaching in geometry and measures should consolidate and extend knowledge developed in number. Teaching should also ensure that pupils classify shapes with increasingly complex geometric properties and that they learn the vocabulary they need to describe them.

By the end of year 6, pupils should be fluent in written methods for all four operations, including long multiplication and division, and in working with fractions, decimals and percentages. Pupils should read, spell and pronounce mathematical vocabulary correctly.

Number - Number and Place Value

Reception	Year 1	Year 2	Year 3	Year 4	Y
			Cou	nting	
*Rote count from 1	*Count to and across 100, forwards and backwards, beginning with 0 or 1, or from	*Count in steps of 2, 3, and 5 from 0, and in tens from any number, forward and	*Count from 0 in multiples of 4, 8, 50 and 100	*Count in multiples of 6, 7, 9, 25 and 1000	*Count forwa in steps of po given numbe
*Rote count on from a given number between 1 and 20	any given number	backward	*Count up and down in tenths	*Count backwards through zero to include negative	*Count forwa
*Count back from 20 to 0	*Count in multiples of twos, fives and tens			numbers	backwards in
*Rote count back from a given number between 0 and 20				*Count up and down in hundredths	
*Know what number comes between two given numbers					
*Rote count beyond 20					
*Understand that counting is to find out how many					
*Use one to one correspondence when counting					
*Understand the last number said is the number in the set					
*Count up to 20 objects, pictures, sounds and actions					
*Understand and use conservation of number					
*Use the word 'zero' to represent 'none'					
*State without counting (subitise) quantities within 5					

Year 5	Year 6				
ards or backwards owers of 10 for any er up to 1 000 000	*Count forwards or backwards in steps of integers, decimals or powers of 10 for any number				
ards and in decimal steps					

Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
			Place Value			
*Recognise and identify numerals 0 to 20	*Read and write numbers to 100 in numerals	*Read and write numbers to at least 100 in numerals and in words	*Read and write numbers up to 1000 in numerals and in words	*Read and write numbers to at least 10 000	*Read and write numbers to at least 1 000 000	*Read and write numbers up to 10 000 000
*Represent amounts in their own ways	*Read and write numbers from 1 to 20 in numerals and words		*Read and write numbers with one decimal place	*Read and write numbers with up to two decimal places	*Read and write numbers with up to three decimal places	
*Write numerals 0 to 20						
*Select the numeral that represents a set of objects	*Begin to recognise the place value of numbers beyond 20 (tens and ones)	*Recognise the place value of each digit in a two-digit number (tens, ones)	*Recognise the place value of each digit in a three-digit number (hundreds, tens, ones)	*Recognise the place value of each digit in a four-digit number (thousands, hundreds, tens, and ones)	*Determine the value of each digit in numbers to at least 1 000 000	*Determine the value of each digit in numbers up to 10 000 000
*Partition a set of objects in different ways using the terminology part-part-whole						
*Understand that 'teens'			Identify the value of each digit to one decimal place	Identify the value of each digit to two decimal places	Identify the value of each digit to three decimal	Identify the value of each digit to three decimal
numbers are a group of 10 plus another number *Understand that 20 is the		*Partition numbers in different ways (for example, 23 = 20 + 3 and 23 = 10 + 13)	Partition numbers in different ways (for example, 146 = 100 + 40 + 6 & 146 = 130 + 16)	Partition numbers in different ways (for example, 2.3 = 2 + 0.3 and 2.3 = 1 + 1.3)	places	places
same as two groups of 10	*Identify and represent numbers using objects and pictorial representations including the number line	*Identify, represent and estimate numbers using different representations, including the number line	*Identify, represent and estimate numbers using different representations, including the number line	*Identify, represent and estimate numbers using different representations, including the number line	*Identify, represent and estimate numbers using the number line	*Identify, represent and estimate numbers using the number line
*Compare two sets of	*Use the language of: equal	*Compare and order numbers	Comparing and ordering *Compare and order numbers	*Order and compare numbers	*Order and compare numbers	*Order and compare numbers
different objects saying which set is more, greater, fewer, less, same, equal	to, more than, less than (fewer), most, least	from 0 up to 100; use <, > and = signs	up to 1000 *Compare and order numbers with one decimal place	*Order and compare numbers with the same number of	to at least 1 000 000 *Order and compare numbers	up to 10 000 000 *Order and compare numbers
*Order three or more sets of objects			with one decimal place	decimal places up to two decimal places	with up to three decimal places	including integers, decimals and negative numbers
*Order numerals 0 to 20	*Given a number, identify one more and one less	*Find 1 or 10 more or less than a given number	*Find 1, 10 or 100 more or less than a given number	*Find 0.1, 1, 10, 100 or 1000 more or less than a given number	*Find 0.01, 0.1, 1, 10, 100, 1000 and other powers of 10 more or less than a given number	*Find 0.001, 0.01, 0.1, 1, 10 and powers of 10 more or less than a given number
		Round	ling, approximation and esti	imation		
*Make a sensible guess of quantities within 10		*Round numbers to at least 100 to the nearest 10	*Round numbers to at least 1000 to the nearest 10 or 100	*Round any number to the nearest 10, 100 or 1000	*Round any number up to 1 000 000 to the nearest 10, 100, 1000, 10 000 and 100 000	*Round any whole number to a required degree of accuracy
				*Round decimals with one decimal place to the nearest whole number	*Round decimals with two decimal places to the nearest whole number and to one decimal place.	*Round decimals with three decimal places to the nearest whole number or one or two decimal places

Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
	1		Multiplying by powers of 10		1	1
		*Understand the connection between the 10 multiplication table and place value	*Find the effect of multiplying a one- or two-digit number by 10 and 100, identify the value of the digits in the answer	*Find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths	*Multiply and divide whole numbers and those involving decimals by 10, 100 and 1000	*Multiply and divide numbers by 10, 100 and 1000 giving answers up to three decimal places
			Negative numbers			
				*Count backwards through zero to include negative numbers (see counting)	*Interpret negative numbers in context, count forwards and backwards with positive and negative whole numbers through zero	*Use negative numbers in context, and calculate intervals across zero
			Sequences and patterns			
*Explore and represent the patterns in odd and even numbers *Recognise repeating patterns in the counting sequence i.e. 6, 7, 8, 9 and 16, 17, 18, 19 and 26, 27, 28, 29 etc.	*Recognise and create repeating patterns with numbers, objects and shapes *Identify odd and even numbers linked to counting in twos from 0 and 1	*Describe and extend simple sequences involving counting on or back in different steps	*Describe and extend number sequences involving counting on or back in different steps	*Describe and extend number sequences involving counting on or back in different steps, including sequences with multiplication and division steps	*Describe and extend number sequences including those with multiplication and division steps and those where the step size is a decimal	*Describe and extend number sequences including those with multiplication and division steps, inconsistent steps, alternating steps and those where the step size is a decimal
	L	L	Roman numerals		L	
			*Read Roman numerals from I to XII (see time)	*Read Roman numerals to 100 (I to C) and know that over time, the numeral system changed to include the concept of zero and place value	*Read Roman numerals to 1000 (M) and recognise years written in Roman numerals	
			Solving num	ber problems		
*Represent and explain their thinking in their own ways	*Solve problems and practical problems involving all of the above	*Use place value and number facts to solve problems	*Solve number problems and practical problems involving these ideas	*Solve number and practical problems that involve all of the above and with increasingly large positive numbers	*Solve number problems and practical problems that involve all of the above	*Solve number and practical problems that involve all of the above

Number - Addition and Subtraction

Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
			standing Addition and Subtr	action		
*Understand the concept of addition by practically combining sets of objects to how many and use the terminology part-part-whole *Understand the concept of subtraction by practically removing one amount from within another to find how many are left and use the terminology part-part-whole	*Read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs	*Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting) *Show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot *Understand subtraction as take away and difference (how many more, how many	*Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method) *Understand and use take away and difference for subtraction, deciding on the most efficient method for the numbers involved, irrespective of context	*Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method)	*Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method)	*Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known fact, calculate mentally, use a jotting, written method)
		less/fewer)	Addition and subtraction fac	ta		
*Automatically recall addition and subtraction facts up to 5 and some addition and	*Represent and use number bonds and related subtraction facts within 20	*Recall and use addition and subtraction facts to 20 fluently, and derive and use related	*Recall and use addition and subtraction facts for 100 (multiples of 5 and 10)	*Recall and use addition and subtraction facts for 100	*Recall and use addition and subtraction facts for 1 and 10 (with decimal numbers to one	*Recall and use addition and subtraction facts for 1 (with decimal numbers to two
subtraction facts to 10 *Identify one more and one less than a given number		facts up to 100 *Recall and use number bonds for multiples of 5	*Derive and use addition and subtraction facts for 100	*Recall and use addition and subtraction facts for multiples of 100 totalling 1000	decimal place) *Derive and use addition and subtraction facts for 1 (with	decimal places)
*Identify two more and two less than a given number		totalling 60 (to support telling time to nearest 5 minutes)	*Derive and use addition and subtraction facts for multiples of 100 totalling 1000	*Derive and use addition and subtraction facts for 1 and 10 (with decimal numbers to one decimal place)	decimal numbers to two decimal places)	
			Mental Calculation			
*Add two single-digit numbers totalling up to 10, using practical equipment		*Select a mental strategy appropriate for the numbers involved in the	*Select a mental strategy appropriate for the numbers involved in the	*Select a mental strategy appropriate for the numbers involved in the	*Select a mental strategy appropriate for the numbers involved in the	*Select a mental strategy appropriate for the numbers involved in the
*Add two single-digit numbers totalling greater than 10, using practical equipment	*Add and subtract one-digit and two-digit numbers to 20, including zero (using concrete objects and pictorial representations)	*Add and subtract numbers using concrete objects, pictorial representations, and mentally, including: - a two-digit number and	*Add and subtract numbers mentally, including: -a three-digit number and ones	*Add and subtract mentally combinations of two and three digit numbers and decimals to one decimal place	*Add and subtract numbers mentally with increasingly large numbers and decimals to two decimal places	*Perform mental calculations, including with mixed operations and large numbers and decimals
*Subtract a single-digit number from a number up to 10, using practical equipment *Subtract a single-digit		ones - a two-digit number and tens -adding three one-digit numbers	-a three-digit number and tens -a three-digit number and hundreds			
number from a number greater than 10, using practical equipment						
	I		Written Methods	I	I	L
	*Written methods are informal at this stage – see mental methods for expectation of calculations	*Written methods are informal at this stage – see mental methods for expectation of calculations	*Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction	*Add and subtract numbers with up to 4 digits and decimals with one decimal place using the formal written methods of columnar addition and subtraction where appropriate	*Add and subtract whole numbers with more than 4 digits and decimals with two decimal places, including using formal written methods (columnar addition and subtraction)	*Add and subtract whole numbers and decimals using formal written methods (columnar addition and subtraction)

Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
·		Estim	nating and checking calcul	lations		·
*Relate subtraction and addition in practical situations using the terminology part- part-whole		*Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems	*Estimate the answer to a calculation and use inverse operations to check answers	*Estimate and use inverse operations to check answers to a calculation	*Use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy	*Use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy
			Order of operations			
						Use their knowledge of the order of operations to carry out calculations involving the four operations
		Solving addition and subt	raction problems including	those with missing numbers		
*Represent and explain their thinking in their own ways	*Solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as $7 = \Box - 9$	*Solve problems with addition and subtraction including those with missing numbers: -using concrete objects and pictorial representations, including those involving numbers, quantities and measures -applying their increasing knowledge of mental and written methods	*Solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction	*Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why *Solve addition and subtraction problems involving missing numbers	*Solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why *Solve addition and subtraction problems involving missing numbers	*Solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why *Solve problems involving addition, subtraction, multiplication and division, including those with missing numbers

Number – Multiplication and Division

Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
		Unders	standing multiplication and o	division		
*Understand that sharing is splitting an amount into equal parts *Understand that halving is splitting into two equal parts *Understand that doubling is adding a number to itself		*Understand multiplication as repeated addition *Understand division as sharing and grouping and that a division calculation can have a remainder *Show that multiplication of two numbers can be done in any order (commutative) and division of one number by	*Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known or related fact, calculate mentally, use a jotting, written method) *Understand that division is the inverse of multiplication and vice versa *Understand how multiplication and division statements can be represented using arrays *Understand division as sharing and grouping and use	*Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known or related fact, calculate mentally, use a jotting, written method) *Recognise and use factor pairs and commutativity in mental calculations	*Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known or related fact, calculate mentally, use a jotting, written method) *Identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers	*Choose an appropriate strategy to solve a calculation based upon the numbers involved (recall a known or related fact, calculate mentally, use a jotting, written method)
		another cannot	each appropriately			
			ultiplication and division fac	ats		
		*Recall and use multiplication	*Recall and use multiplication	*Recall multiplication and	*Know and use the	*Identify common factors,
		and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers	and division facts for the 3, 4 and 8 multiplication tables	division facts for multiplication tables up to 12 × 12	 vocabulary of prime numbers, prime factors and composite (nonprime) numbers *Establish whether a number up to 100 is prime and recall prime numbers up to 19 *Recognise and use square numbers and cube numbers, and the notation for squared (²) and cubed (³) 	common multiples and prime numbers
*Automatically recall double facts to double 5	*Recall and use doubles of all numbers to 10 and corresponding halves	*Derive and use doubles of simple two-digit numbers (numbers in which the ones total less than 10) *Derive and use halves of simple two-digit even numbers (numbers in which the tens are even)	*Derive and use doubles of all numbers to 100 and corresponding halves *Derive and use doubles of all multiples of 50 to 500	*Use partitioning to double or halve any number, including decimals to one decimal place	*Use partitioning to double or halve any number, including decimals to two decimal places	*Use partitioning to double or halve any number
		,	Mental methods			
		*Calculate mathematical statements for multiplication (using repeated addition) and division within the multiplication tables and write them using the multiplication (×), division (÷) and equals (=) signs	*Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one- digit numbers, using mental methods	*Use place value, known and derived facts to multiply and divide mentally, including: - multiplying by 0 and 1 - dividing by 1 - multiplying together three numbers	*Multiply and divide numbers mentally drawing upon known facts *Solve problems involving multiplication and division including using their knowledge of factors and multiples, squares and cubes	*Perform mental calculations, including with mixed operations and large numbers

Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
			Written methods			
	*Written methods are informal at this stage – see mental methods for expectation of calculations	*Written methods are informal at this stage – see mental methods for expectation of calculations	*Write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, progressing to formal written methods	*Multiply two-digit and three- digit numbers by a one-digit number using formal written layout	*Multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers	*Multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication *Multiply one-digit numbers with up to two decimal places by whole numbers
			*Write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers divided by one-digit numbers, progressing to formal written methods	*Divide numbers up to 3 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context	*Divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context	*Divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context *Use written division methods in cases where the answer has up to two decimal places
		Estim	nating and checking calcul	ations		
			*Use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy	*Use estimation and inverse to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy	*Use estimation and inverse to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy	*Use estimation and inverse to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy
			Order of operations			
						*Use their knowledge of the order of operations to carry out calculations involving the four operations
		Solving multiplication and	division problems including	those with missing numbers		
	*Solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher	*Solve problems involving multiplication and division (including those with remainders), using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts	*Solve problems, including missing number problems, involving multiplication and division (and interpreting remainders), including positive integer scaling problems and correspondence problems in which n objects are connected to m objects	*Solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, division (including interpreting remainders), integer scaling problems and harder correspondence problems such as n objects are connected to m objects	*Solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign *Solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates	*Solve problems involving addition, subtraction, multiplication and division

Number – Fractions (including decimals and percentages)

Reception	Year 1	Year 2	Year 3	Year 4	Ye
· ·			Understanding fractions	•	
*Understand that sharing is splitting an amount into equal parts	*Understand that a fraction can describe part of a whole *Understand that a unit fraction represents one equal part of a whole	*Understand and use the terms numerator and denominator *Understand that a fraction can describe part of a set *Understand that the larger the denominator is, the more pieces it is split into and therefore the smaller each	*Show practically or pictorially that a fraction is one whole number divided by another (for example, ³ / ₄ can be interpreted as ⁴ / ₃ ÷ 4) *Understand that finding a fraction of an amount relates to division	*Understand that a fraction is one whole number divided by another (for example, $\frac{3}{4}$ can be interpreted as $3 \div 4$)	
		part will be	· · · · · · · · · · · · · · · · · · ·		
*Understand that halving is splitting into two equal parts	*Recognise, find and name a half as one of two equal parts of an object, shape or quantity (including measure) *Recognise, find and name a	*Recognise, find, name and write fractions $\frac{1}{3}$, $\frac{1}{4}$, $\frac{2}{4}$, $\frac{3}{4}$ of a length, shape, set of objects or quantity	ns of objects, shapes and que *Recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators	*Recognise, find and write fractions of a discrete set of objects including those with a range of numerators and denominators	*Recognise mi and improper convert from c other
	quarter as one of four equal parts of an		*Recognise and use fractions as numbers: unit fractions and non-		*Read and wri
			*Recognise that tenths arise from dividing an object into 10 equal parts and in dividing one-digit numbers or quantities by 10	*Recognise that hundredths arise when dividing an object by a hundred and dividing by ten	numbers as fra (e.g 0.71 + 71/
			g, comparing and ordering		
		*Count on and back in steps of $\frac{1}{2}$ and $\frac{1}{4}$	*Count on and back in steps of $\frac{1}{2}$, $\frac{1}{4}$ and $\frac{1}{3}$	*Count on and back in steps of unit fractions	*Count on and number steps s
			*Compare and order unit fractions and fractions with the same denominators (including on a number line)	*Compare and order unit fractions and fractions with the same denominators (including on a number line) (Continued from Y3)	*Compare and fractions whos denominators multiples of the number (inclue number line)

Year 5	Year 6
nixed numbers	
er fractions and	
n one form to the	
vrite decimal	
ractions	
1/100)	
<u> </u>	
nd back in mixed $\frac{1}{2}$	
s such as $1\frac{1}{2}$	
nd order	*Compare and order
ose	fractions, including fractions 1 (including on a number)
rs are all he same	line)
luding on a	
-	

Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
			Equivalence			
		*Write simple fractions for example, $\frac{1}{2}$ of 6 = 3 and recognise the equivalence of $\frac{2}{4}$ and $\frac{1}{2}$	*Recognise and show, using diagrams, equivalent fractions with small denominators	*Recognise and show, using diagrams, families of common equivalent fractions	*Identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths	*Use common factors to simplify fractions; use common multiples to express fractions in the same denomination
				*Recognise and write decimal equivalents of any number of tenths or hundredths	*Recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents	*Recall and use equivalences between simple fractions, decimals and percentages, including in different contexts
				*Recognise and write decimal equivalents to $\frac{1}{4}$, $\frac{1}{2}$, $\frac{3}{4}$		*Associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. $\frac{3}{8}$)
			Calculating with fractions			
			*Add and subtract fractions with the same denominator within one whole (using diagrams) (for example, $\frac{5}{7} + \frac{1}{7}$ = $\frac{6}{7}$)	*Add and subtract fractions with the same denominator (using diagrams)	*Add and subtract fractions with the same denominator and denominators that are multiples of the same number (using diagrams) Write mathematical statements >1 as a mixed number (e.g. $\frac{2}{5} + \frac{4}{5} = \frac{6}{5} = 1\frac{1}{5}$) *Multiply proper fractions and	*Add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions *Multiply simple pairs of
					mixed numbers by whole numbers, supported by materials and diagrams	proper fractions, writing the answer in its simplest form (using diagrams) (e.g. $\frac{1}{4} \times \frac{1}{2} = \frac{1}{8}$) *Divide proper fractions by whole numbers (using
						diagrams)
			Percentages			$(e.g. \frac{1}{3} \div 2 = \frac{1}{6})$
					*Recognise the per cent symbol (%) and understand that per cent relates to 'number of parts per hundred', and write percentages as a fraction with denominator 100, and as a decimal	*Find simple percentages of amounts

Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6				
Solving problems involving fractions, decimals and percentages										
			*Solve problems that involve all of the above	*Solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number	*Solve problems involving fractions	*Solve problems involving fractions				
				*Solve simple measure and money problems involving fractions and decimals to two decimal places	*Solve problems involving number up to three decimal places	*Solve problems which require answers to be rounded to specified degrees of accuracy				
					*Solve problems which require knowing percentage and decimal equivalents $\begin{array}{c} \text{of} \\ \frac{1}{2} \frac{1}{4} \frac{1}{5} \frac{2}{5} \frac{4}{5} \\ \text{with a denominator of a} \\ \text{multiple of 10 or 25} \end{array}$	*Solve problems involving the calculation of percentages (for example, of measures, and such as 15% of 360) and the use of percentages for comparison				

Ratio and proportion

Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6			
	Ration and proportion								
						*Solve problems involving the relative sizes of two quantities where missing values can be found using integer multiplication and division facts			
						*Solve problems involving unequal sharing and grouping using knowledge of fractions and multiples			
						*Solve problems involving similar shapes where the scale factor is known or can be found			

<u>Algebra</u>

Ration and proportion					
				*Express missing number problems algebraically Use simple formulae	
				*Generate and describe linear number sequences	
				*Find pairs of numbers that satisfy an equation with two unknowns	
				*Enumerate possibilities of combinations of two variables	

Measurement (length/height, perimeter, area and mass/weight)

Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
			Length/height			
*Understand that measures of distance can have different names including length, width, height *Understand and use language to compare the length/width of two objects	*Measure and begin to record lengths and heights, using nonstandard and then manageable standard units (m and cm) within children's range of counting competence	*Choose and use appropriate standard units to estimate and measure length/height in any direction (m/cm) to the nearest appropriate unit using rulers	*Measure, add and subtract lengths (m/cm/mm)	*Estimate and calculate lengths	*Use, read and write standard units of length to a suitable degree of accuracy	*Use, read and write standard units of length using decimal notation to three decimal places
*Understand and use language to compare the height of two objects	*Compare and describe lengths and heights (for example, long/short, longer/shorter, tall/short, double/half)	*Compare and order lengths and record the results using >, < and =	*Compare lengths (m/cm/mm)	*Compare lengths	*Understand and use approximate equivalences between metric and common imperial units such as inches	
*Understand and use language of comparison when ordering three objects of different lengths/widths/heights						
*Understand the concept of the conservation of length/width/height						
			Perimeter			
			*Understand that perimeter is a measure of distance around the boundary of a shape *Measure the perimeter of	*Measure and calculate the perimeter of a rectilinear figure (including squares) in centimetres and metres	*Measure and calculate the perimeter of composite rectilinear shapes in centimetres and metres	*Recognise that shapes with the same areas can have different perimeters and vice versa
			simple 2-D shapes			
			Area			
				*Understand that area is a measure of surface within a given boundary	*Calculate and compare the area of rectangles (including squares), and including using standard units, square	*Calculate the area of parallelograms and triangles
				*Find the area of rectilinear shapes by counting squares	centimetres (cm ²) and square metres (m ²) and estimate the area of irregular shapes	*Recognise when it is possible to use the formulae for area and volume of shapes
			Mass			
*Understand the measurement of weight/mass (heavy/light) *Understand and use	*Measure and begin to record mass/weight, using non-standard and then standard units (kg and g) within children's range of counting competence	*Choose and use appropriate standard units to estimate and measure mass (kg/g) to the nearest appropriate unit using scales	*Measure, add and subtract mass (kg/g)	*Estimate and calculate mass	*Use, read and write standard units of mass to a suitable degree of accuracy	*Use, read and write standard units of mass using decimal notation to three decimal places
language to compare the weight/mass of two objects *Understand the concept of conservation of weight/mass	*Compare and describe mass/weight (for example, heavy/light, heavier than, lighter than)	*Compare and order mass and record the results using >, < and =	*Compare mass (kg/g)	*Compare mass	*Understand and use approximate equivalences between metric and common imperial units such as pounds	

Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
		1	Capacity/volume			
*Understand the measurement of volume/ capacity (empty/full/nearly) *Understand and use language to compare two of the same container holding different amounts *Understand and use the language of comparison when ordering three of the same container holding different amounts *Understand the concept of the conservation of volume/capacity	*Measure and begin to record capacity and volume using nonstandard and then standard units (litres and ml) within children's range of counting competence *Compare and describe capacity and volume (for example, full/empty, more than, less than, half, half full, quarter)	*Choose and use appropriate standard units to estimate and measure capacity and volume (litres/ml) to the nearest appropriate unit using measuring vessels *Compare and order volume/capacity and record the results using >, < and =	*Measure, add and subtract volume/capacity (I/mI) *Compare volume/capacity (I/mI)	Estimate and calculate volume/capacity *Compare volume capacity	*Estimate (and calculate) volume (for example, using 1 cm ³ blocks to build cuboids (including cubes)) and capacity (for example, using water) *Understand the difference between liquid volume, including capacity and solid volume *Understand and use approximate equivalences between metric and common imperial units such as pints	*Use, read and write standard units of volume using decimal notation to three decimal places *Calculate and estimate volume of cubes and cuboids using standard units, including cubic centimetres (cm ³) and cubic metres (m ³) and extending to other units (for example, mm ³ and km ³) *Compare volume of cubes and cuboids using standard units, including cubic centimetres (cm ³) and cubic metres (m ³) and extending to other units (for example, mm ³ and km ³)
			Temperature			
		*Choose and use appropriate standard units to estimate and measure temperature to the nearest degree (°C) using thermometers	*Continue to estimate and measure temperature to the nearest degree (°C) using thermometers	*Order temperatures including those below 0°C	*Continue to order temperatures including those below 0°C	*Calculate differences in temperature, including those that involve a positive and negative temperature
			Conversion			
				*Convert between different units of measure (e.g. kilometre to metre; hour to minute)	*Convert between different units of metric measure (for example, kilometre and metre; centimetre and metre; centimetre and millimetre; gram and kilogram; litre and millilitre)	*Convert between standard units, converting measurements of length, mass, volume and time from a smaller unit of measure to a larger unit, and vice versa, using decimal notation to three decimal places *Convert between miles and

Measurement (time)

Reception	Year 1	Year 2	Year 3	Year 4	Ye
			Time		
*Talk about significant times of the day, e.g. home time, lunch time, snack time, bed time, etc. *Know the names of the days of the week	*Recognise and use language relating to dates, including days of the week, weeks, months and years *Compare and describe time	*Compare and sequence	*Record and compare time in	*Convert between	*Convert betw
*Say the names of the days of the week in order *Understand and use language – before, after, yesterday, today, tomorrow *Use the language of comparison when talking	(for example, quicker, slower, earlier, later) *Sequence events in chronological order using language (for example, before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening	intervals of time	terms of seconds, minutes and hours; use vocabulary such as o'clock, a.m./p.m., morning, afternoon, noon and midnight	different units of time, e.g. hour to minute	time in a prob context
about time, e.g. longer/ shorter; faster/slower *Sequence two or three familiar events and describe	*Measure and begin to record time (hours, minutes, seconds)	*Know the number of minutes in an hour and the number of hours in a day	*Know the number of seconds in a minute, and the number of days in each month, year and leap year	*Read, write and convert time between analogue and digital 12 and 24 hour clocks	*Continue to r convert time k analogue and 24 hour clocks
the sequence	*Tell the time to the hour and half past the hour and draw the hands on a clock face to show these times	* Tell and write the time to five minutes, including quarter past/to the hour and draw the hands on a clock face to show these times	* Tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24- hour clocks		
			*Estimate and read time with increasing accuracy to the nearest minute		
			*Compare durations of events (for example to calculate the time taken by particular events or tasks)		

Year 5	Year 6
tween units of oblem solving	
o read, write and e between nd digital 12 and ks	*Use, read and write standard units of time

Measurement (money and solving problems)

Reception	Year 1	Year 2	Year 3	Year 4	Ye
			Money		
*Understand that we need to pay for goods *Talk about things they want to spend their money on	*Recognise and know the value of different denominations of coins and notes	*Recognise and use symbols for pounds (£) and pence (p)	*Continue to recognise and use symbols for pounds (£) and pence (p) and understand that the decimal point separates pounds and pence	*Write amounts of money using decimal notation	
*Talk about different ways we can pay for things *Recognise that there are different coins		*Combine amounts to make a particular value *Find different combinations of coins that equal the same	*Recognise that ten 10p coins are equivalent to £1 and that each coin is $\frac{1}{10}$ of £1	*Recognise that one hundred 1p coins are equivalent to £1 and that each coin is $\frac{1}{100}$ of £1	
*Recognise 1p coin		amounts of money *Add and subtract money of	*Add and subtract amounts of	*Estimate, compare and calculate money in pounds	
*Use 1p coins to pay for objects		the same unit, including giving change	money to give change, using both £ and p in practical contexts	and pence	
		• •	blems involving money and	1	
	*Solve practical problems for: - lengths and heights - mass/weight - capacity and volume - time	*Solve simple problems in a practical context involving addition and subtraction of money and measures (including time)	*Solve problems involving money and measures and simple problems involving passage of time	*Solve problems involving converting from hours to minutes; minutes to seconds; years to months; weeks to days and problems involving money and measures	*Use all four of solve problem measure (for e mass, volume, decimal notat scaling
					*Solve probler converting be time

Year 5	Year 6
operations to ms involving	*Solve problems involving the calculation and conversion of
r example, length, e, money) using	units of measure (including money and time), using
ation including	decimal notation up to three decimal places where appropriate
ems involving between units of	

Geometry – properties of shapes

Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
			Properties of shape			
*Know that shapes can appear in different ways and be different sizes *Create and describe pictures	*Recognise and name common 2-D shapes, including rectangles (including squares), circles and triangles	*Identify and describe the properties of 2-D shapes, including the number of sides and line symmetry in a vertical line	*Draw 2-D shapes and describe them	*Compare and classify geometric shapes, including quadrilaterals and triangles, based on their properties and sizes	Distinguish between regular and irregular polygons based on reasoning about equal sides and angles	Compare and classify geometric shapes based on their properties and sizes Draw 2-D shapes using given dimensions and angles
using 2-D shapes *Name common 2-D shapes (circle, triangle, square rectangle, oblong rectangle) *Build and make models with 3-D shapes *Name common 3-D shapes (sphere, cube, cuboid)		*Identify 2-D shapes on the surface of 3-D shapes, (for example, a circle on a cylinder and a triangle on a pyramid)	*Identify horizontal and vertical lines and pairs of perpendicular and parallel lines	*Identify lines of symmetry in 2-D shapes presented in different orientations *Complete a simple symmetric figure with *Continue to identify horizontal and vertical lines and pairs of perpendicular and parallel lines	Use the properties of rectangles to deduce related facts and find missing lengths and angles	*Illustrate and name parts of circles, including radius, diameter and circumference and know that the diameter i
*Talk about shapes using mathematical language (straight, curved, sides, flat, solid) *Sort shapes according to	*Recognise and name common 3-D shapes, including cuboids (including cubes), pyramids and spheres	*Identify and describe the properties of 3-D shapes, including the number of edges, vertices and faces	*Make 3-D shapes using modelling materials; recognise 3-D shapes in different orientations and describe them	*Compare and classify geometric shapes based on their properties and sizes	*Identify 3-D shapes, including cubes and other cuboids, from 2-D representations	*Recognise, describe and build simple 3-D shapes, including making nets
their own criteria						
			Angles and rotation			
	*Describe movement, including whole, half, quarter and three-quarter turns	*Use mathematical vocabulary to describe movement, including rotation as a turn	*Recognise angles as a property of shape or a description of a turn			
		* Understand the link between rotation and turns in terms of right angles for quarter, half and three- quarter turns (clockwise and anticlockwise)	*Identify right angles, recognise that two right angles make a half-turn, three make three quarters of a turn and four a complete turn; identify whether angles are greater than or less than a right angle	*Identify acute and obtuse angles and compare and order angles up to two right angles by size	 *Know angles are measured in degrees: estimate and compare acute, obtuse and reflex angles *Draw given angles, and measure them in degrees (°) *Identify: angles at a point and one whole turn (total 360°) -angles at a point on a straight line and ½ a turn (total 180°) -other multiples of 90° 	*Recognise angles where the meet at a point, are on a straight line, or are vertically opposite, and find missing angles *Find unknown angles in any triangles, quadrilaterals, and regular polygons

Geometry – position and direction

Reception	Year 1	Year 2	Year 3	Year 4	Ye
			Patterns		
*Describe and recognise patterns made of objects, numbers and shapes	*Recognise and create repeating patterns with objects and shapes	*Order and arrange combinations of mathematical objects in patterns and sequences			
*Create patterns made of objects, numbers and shapes					
objects, nombers and shapes			Position and direction		
*Understand and use positional language in everyday situations *Understand and use ordinal numbers when describing position	*Describe position and direction	*Use mathematical vocabulary to describe position, movement, including movement in a straight line			
*Understand and use the language of movement/ direction					
		Coordinat	es (including reflection and	t translation)	
			*Describe positions on a square grid labelled with letters and numbers	*Describe positions on a 2-D grid as coordinates in the first quadrant	*Describe pos quadrant of a
				*Plot specified points and draw sides to complete a given polygon	* Plot specified complete sha
				*Describe movements between positions as translations of a given unit to the left/right and up/down	* Identify, deso represent the shape followin translation, usi appropriate lo know that the changed

Year 5	Year 6
positions on the first of a coordinate grid	*Describe positions on the full coordinate grid (all four quadrants)
cified points and shapes	
describe and the position of a lowing a reflection or n, using the ate language, and t the shape has not	* Draw and translate simple shapes on the coordinate plane, and reflect them in the axes

<u>Statistics</u>

Reception	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
			Sorting and classifying			
*Sort shapes according to their own criteria *Sort objects and say what features they have in common	*Sort objects, numbers and shapes to a given criterion and their own	*Compare and sort objects, numbers and common 2-D and 3-D shapes and everyday objects	*Use sorting diagrams to compare and sort objects, numbers and common 2D and 3-D shapes and everyday objects	*Use a variety of sorting diagrams to compare and classify numbers and geometric shapes, including quadrilaterals and triangles, based on their properties and sizes	*Complete and interpret information in a variety of sorting diagrams (including those used to sort properties of numbers and shapes)	*Continue to complete and interpret information in a variety of sorting diagrams (including those used to sort properties of numbers and shapes)
			Present and interpret data			
	*Present and interpret data in block diagrams using practical equipment	*Interpret and construct simple pictograms, tally charts, block diagrams and simple tables	*Interpret and present data using bar charts, pictograms and tables	*Interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs	*Complete, read and interpret information in tables, including timetables	*Interpret and construct pie charts and line graphs and use these to solve problems
			Solve problems using data			
	*Ask and answer simple questions by counting the number of objects in each category *Ask and answer questions by comparing categorical data	*Ask and answer simple questions by counting the number of objects in each category and sorting the categories by quantity *Ask and answer questions about totalling and comparing categorical data	*Solve one-step and twostep questions (for example, 'How many more?' and 'How many fewer?') using information presented in scaled bar charts and pictograms and tables	*Solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs	*Solve comparison, sum and difference problems using information presented in all types of graph including a line graph	*Solve comparison, sum and difference problems using information presented in all types of graph
			Averages			
					*Calculate and interpret the mode, median and range	*Calculate and interpret the mean as an average